

Provably Safe and Efficient Motion Planning with Uncertain Human Dynamics

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<https://safe-dressing.github.io/>

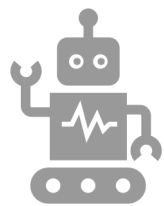
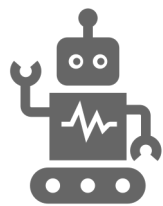
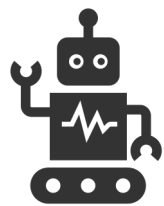
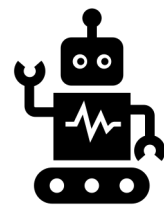


Robot-assisted Dressing



Human
Physical
Safety



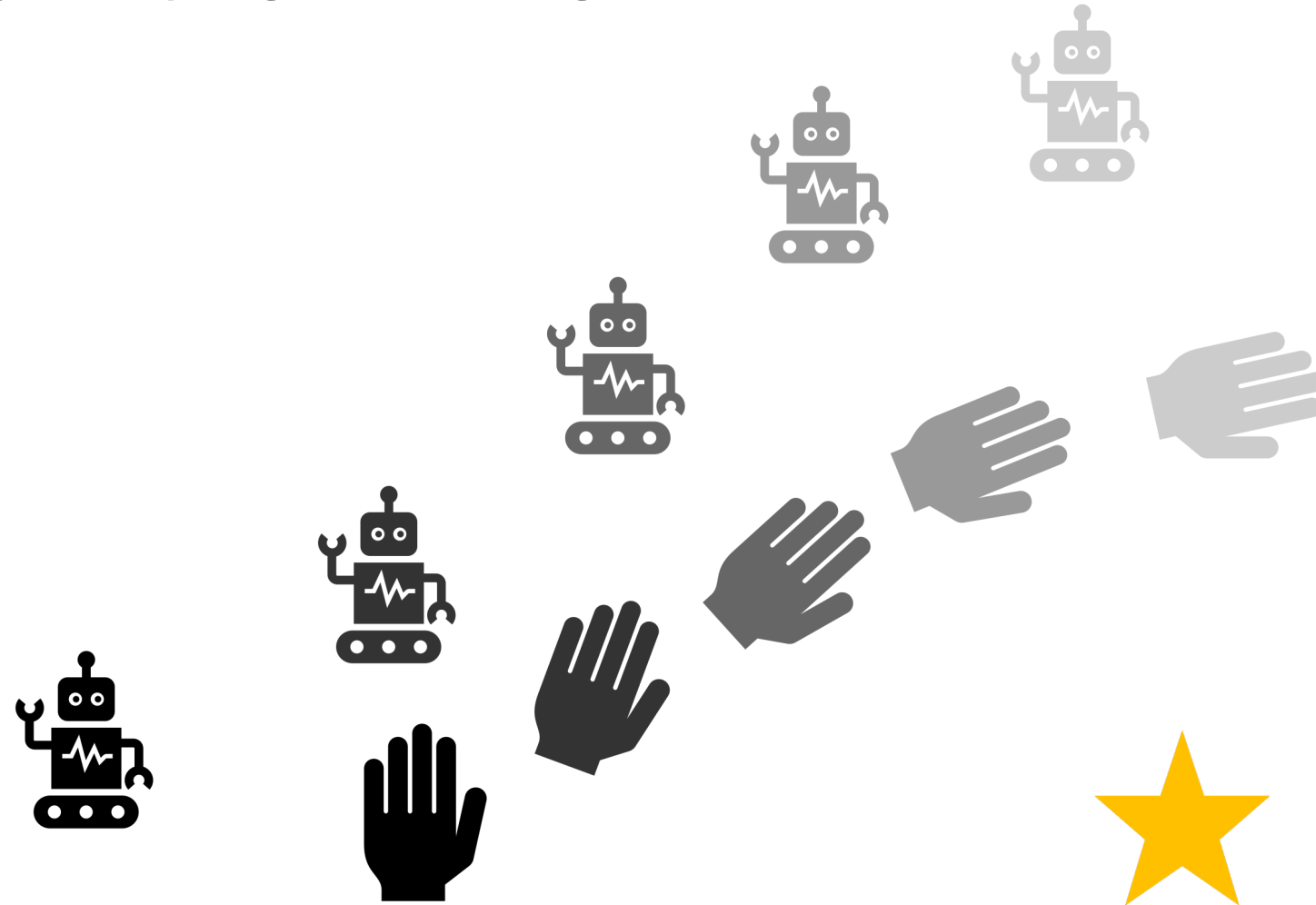


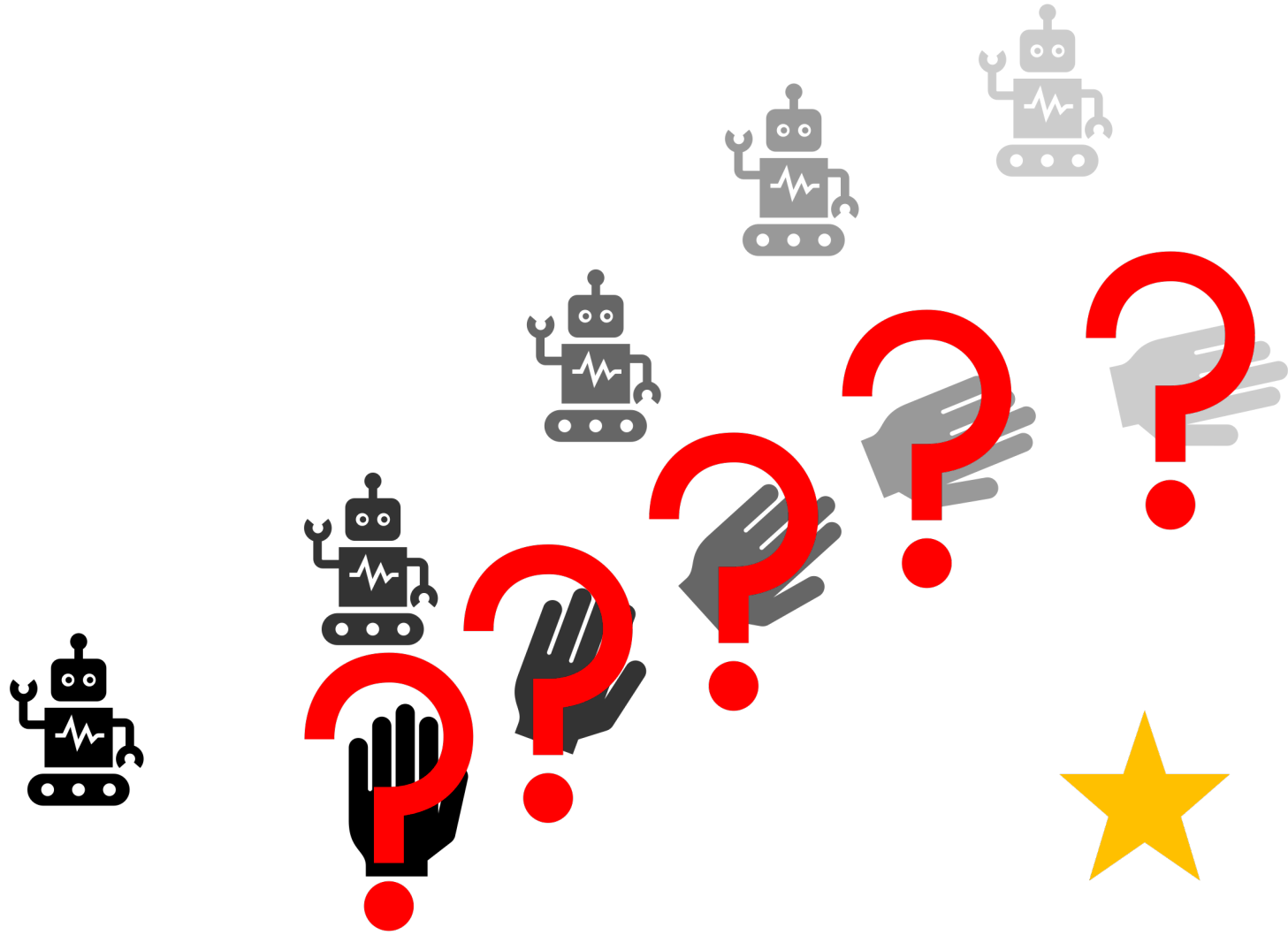
Robot's goal

Robot plan

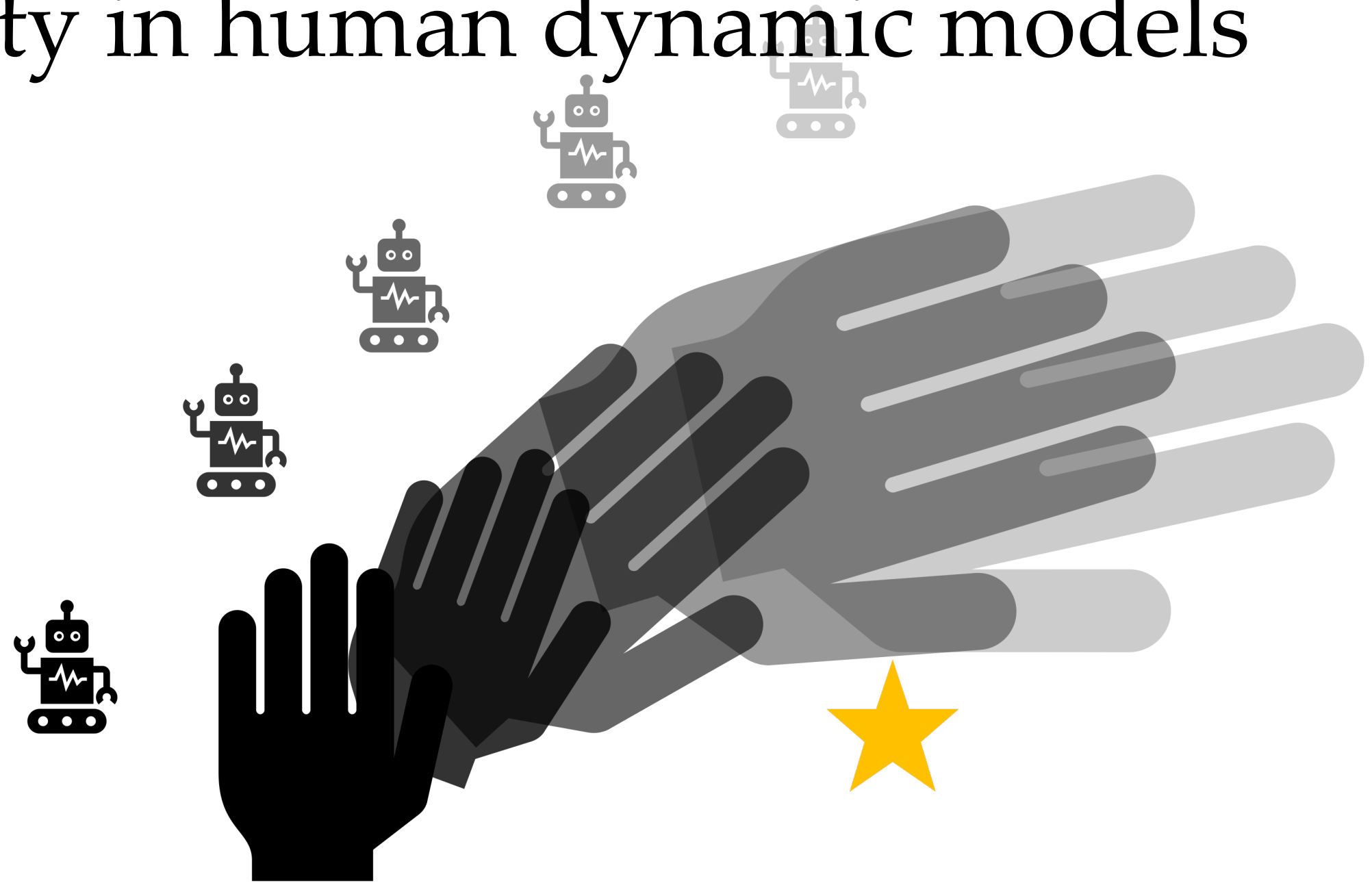
Human-aware motion planners

Safety = collision avoidance





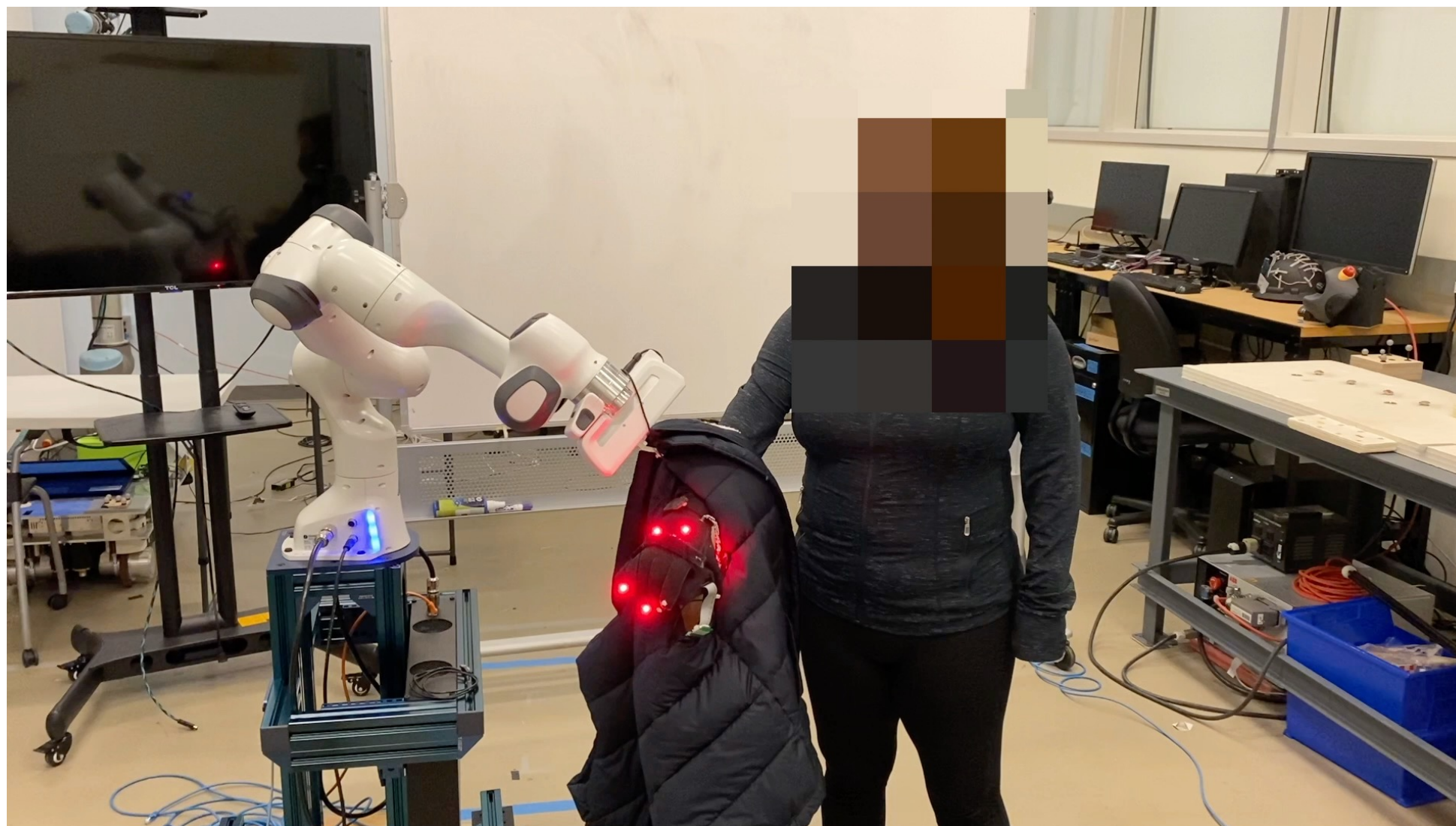
Uncertainty in human dynamic models



Overly conservative
=> **Inefficient**



“Freezing robot problem” under uncertainty





Ensuring **safety** is a **top** priority,
but sometimes,
it comes at the **COST** of **efficiency**

Ensure human *safety*
&& Improve task *efficiency*

Ensure human safety

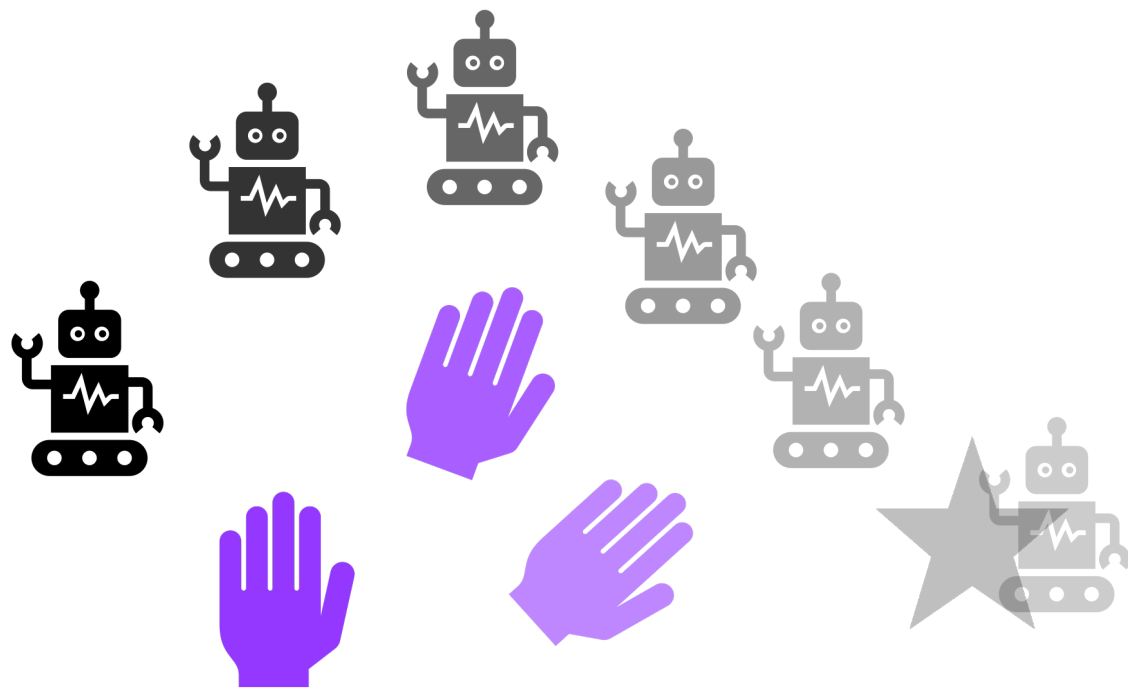
&& Improve task **efficiency**



Collision avoidance
OR safe impact

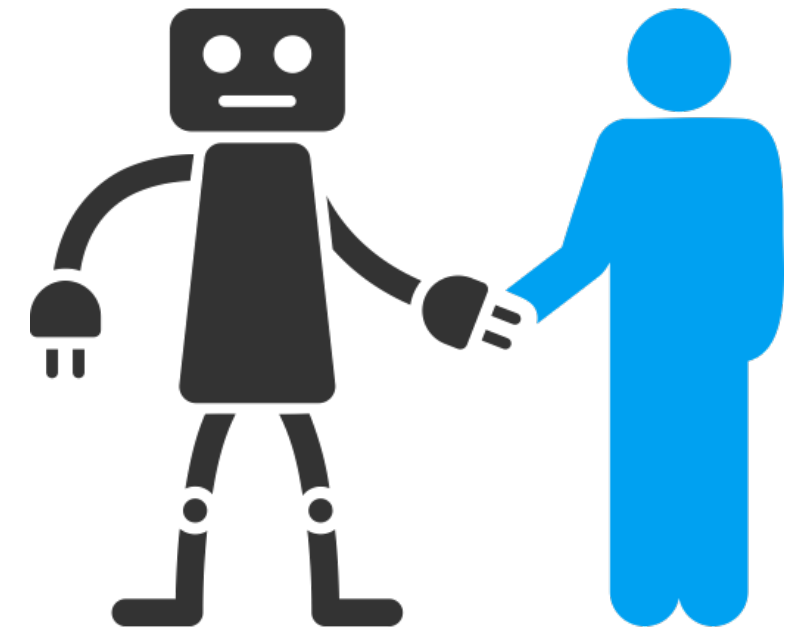
Human-aware motion planners

Collision avoidance



Compliant controllers

Reduce contact force

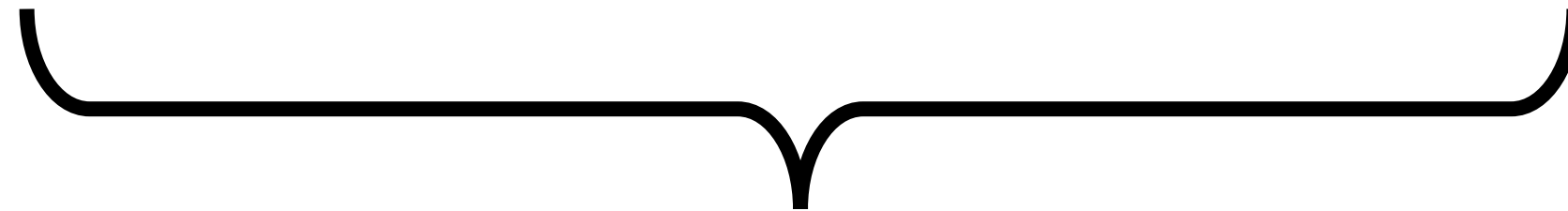


Human-aware motion planners

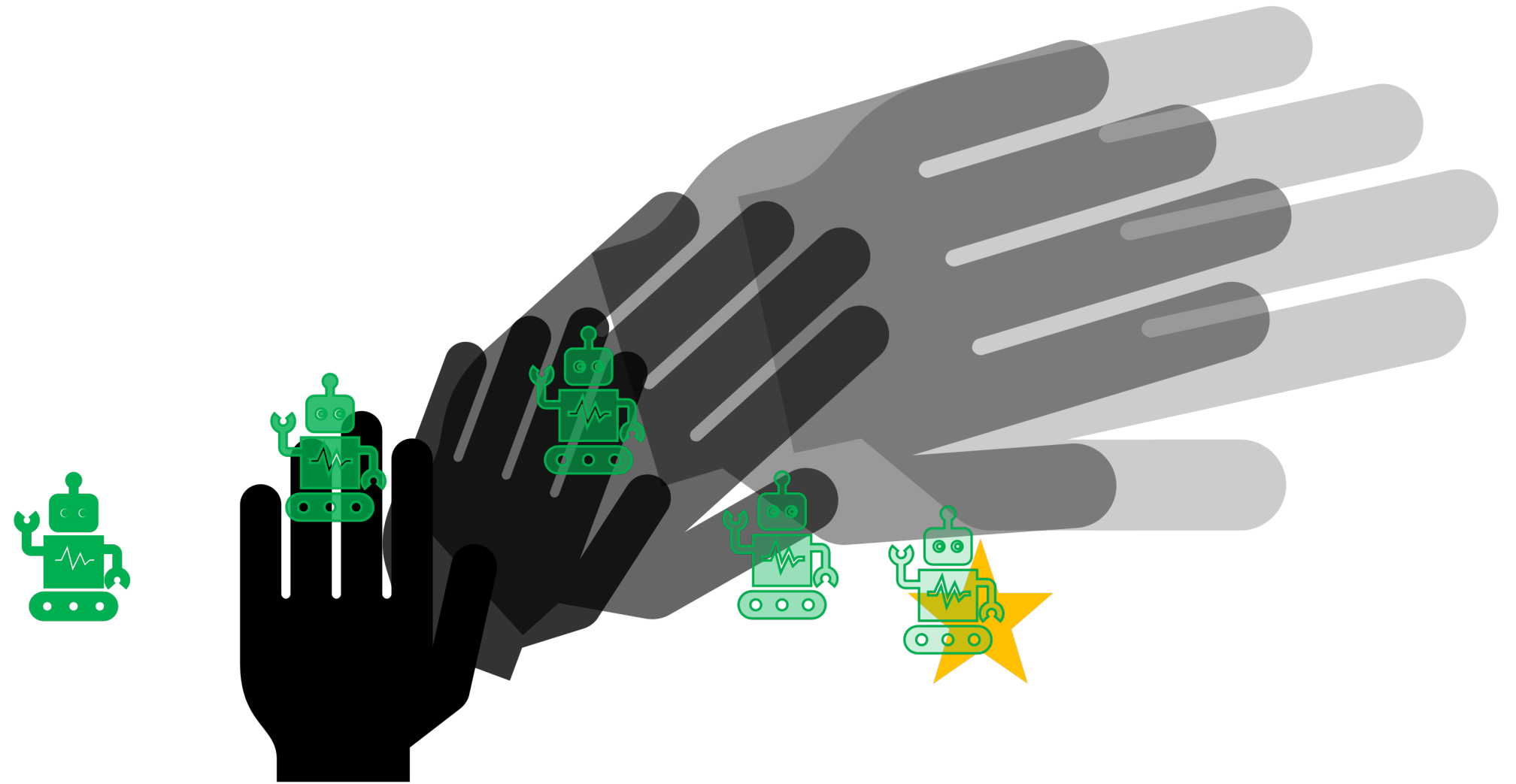
Compliant controllers

Collision avoidance

Reduce contact force



Collision avoidance **OR** safe impact



Ensure human safety

&& Improve task **efficiency**



Collision avoidance
OR safe impact

MPC + high probability
safety guarantee

Ensure human **safety**
&& Improve task **efficiency**

Collision avoidance
OR safe impact

Robot position
at time t

Robot velocity
at time t

$$p_R^t, v_R^t$$



$$p_H^t, v_H^t$$

Human position
at time t

Human velocity
at time t

Assumption: deterministic && “smooth”

Gaussian Process

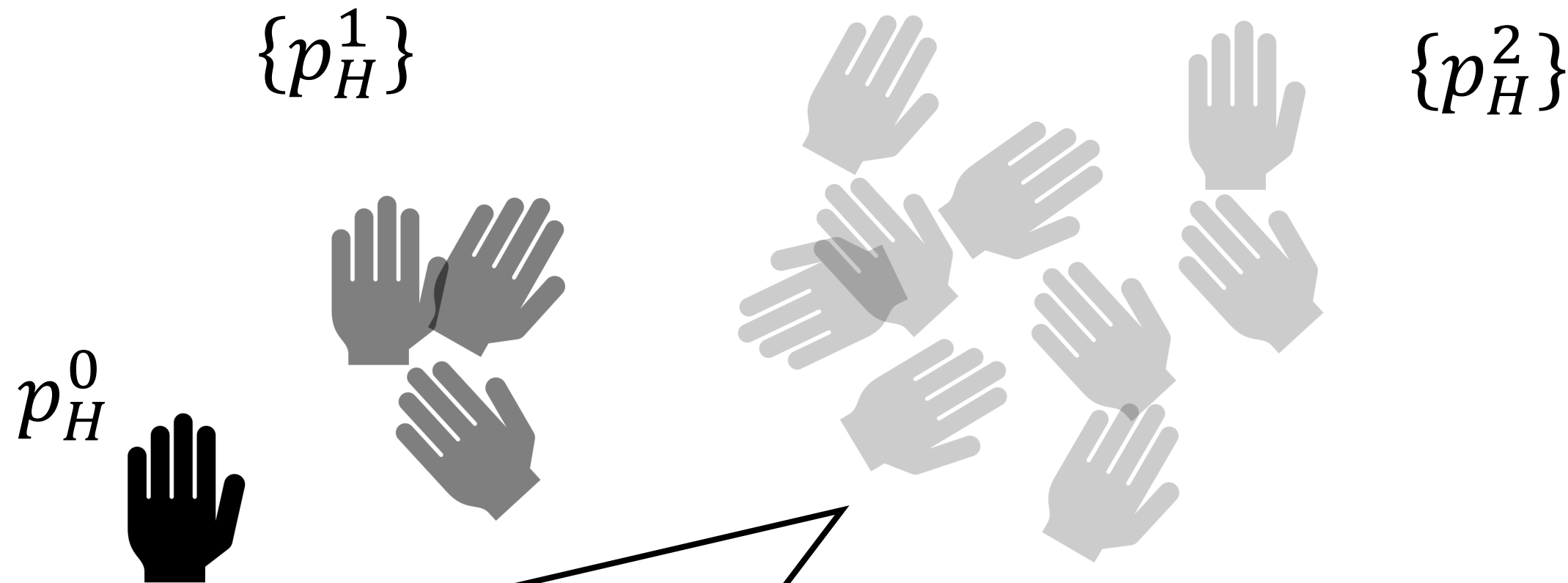
$$p_H^{t+1} = p_H^t + g(p_H^t, p_R^t)$$

$$v_H^{t+1} = \frac{1}{h} (p_H^{t+1} - p_H^t)$$



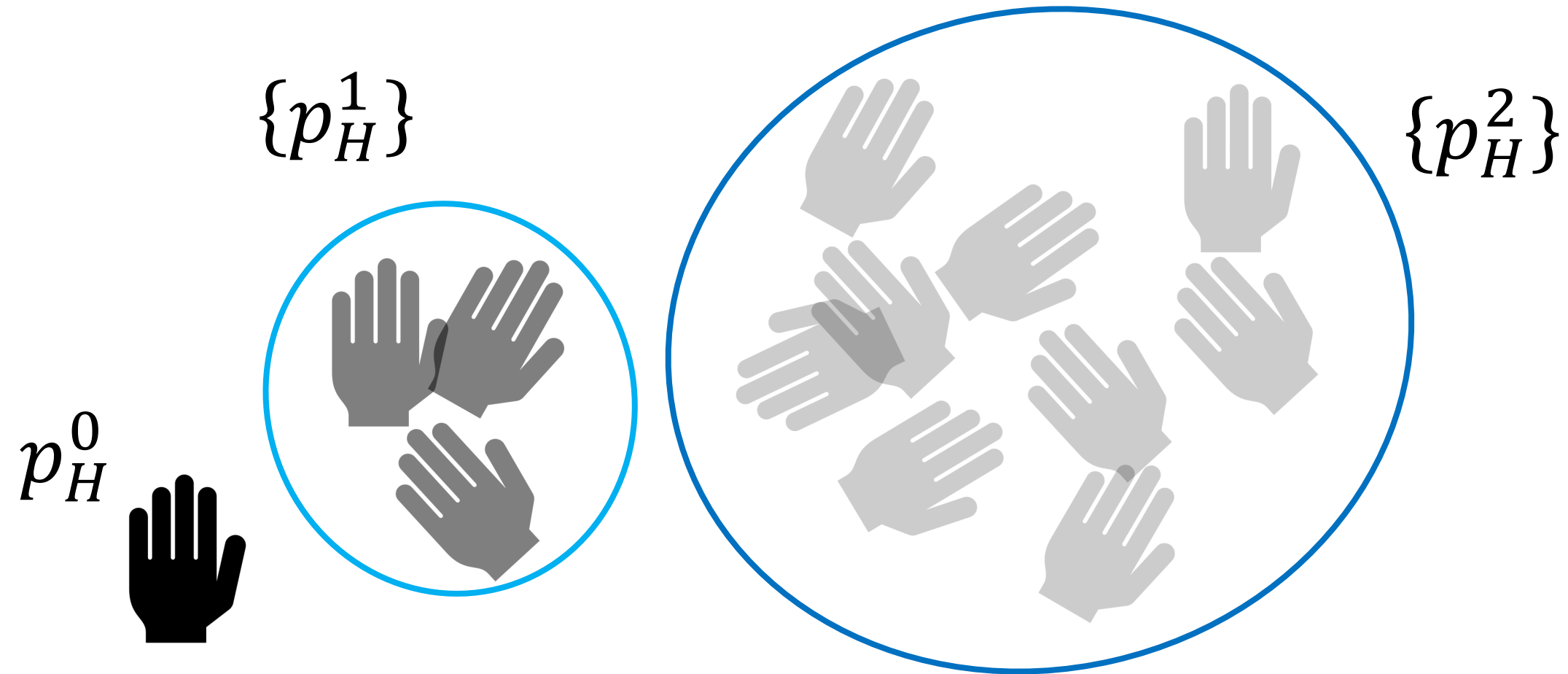
The length of time-steps

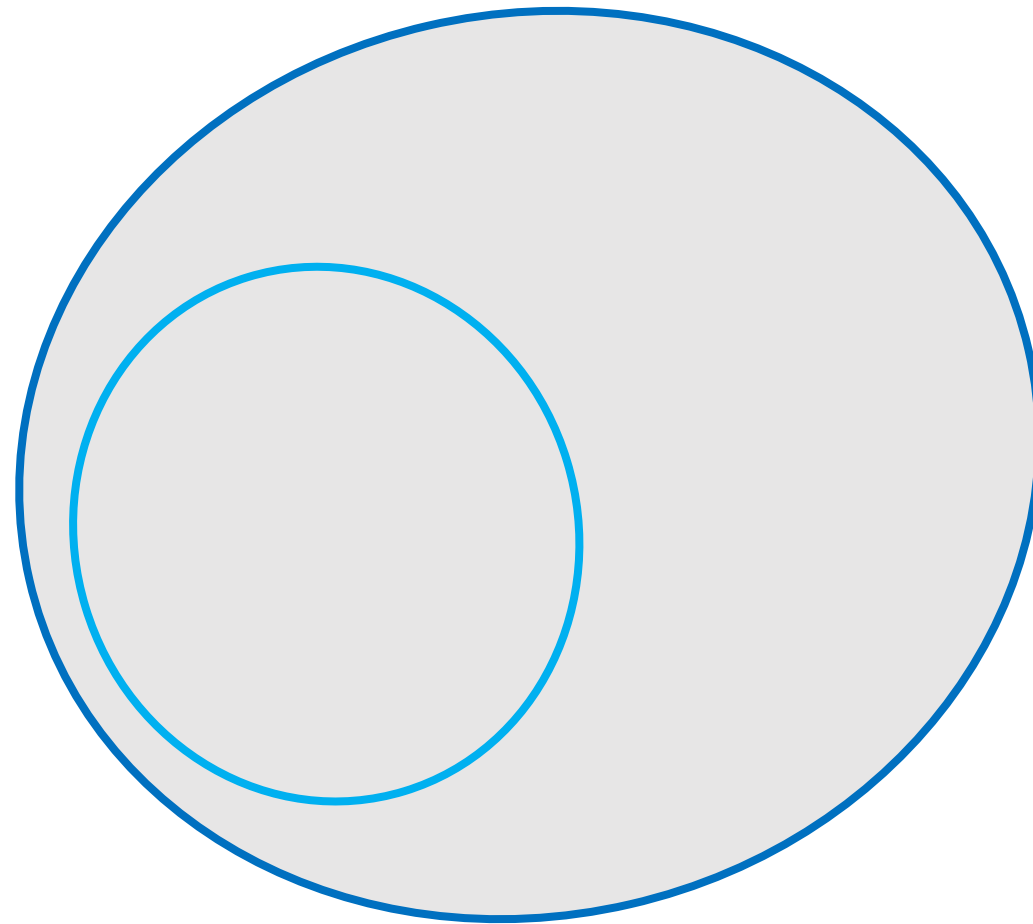
Human motion prediction



Uncertainty in the human dynamic model:

$$p_H^{t+1} = p_H^t + g(p_H^t, p_R^t)$$





Velocity space

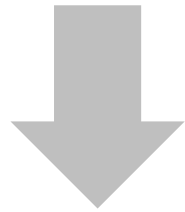
Corollary 1:

.....

With a high probability:

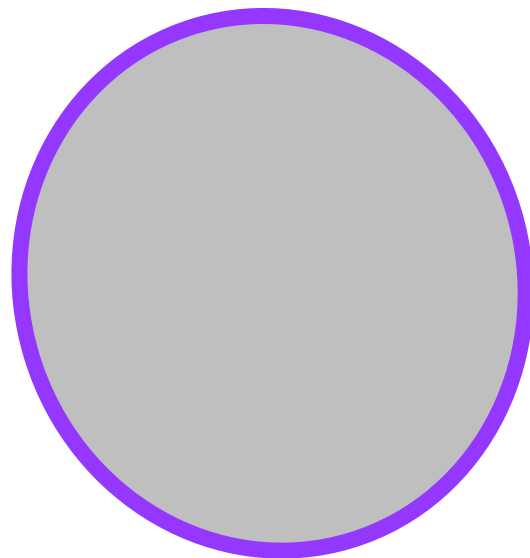
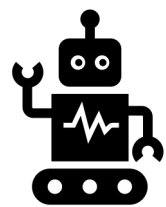
$\forall t \in [1 \dots T]$, human pos, vel \in ellipsoids

Collision avoidance

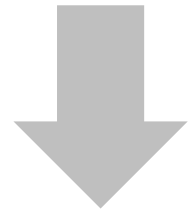


A constraint over

- Robot **pos**
- Human **pos** ellipsoid

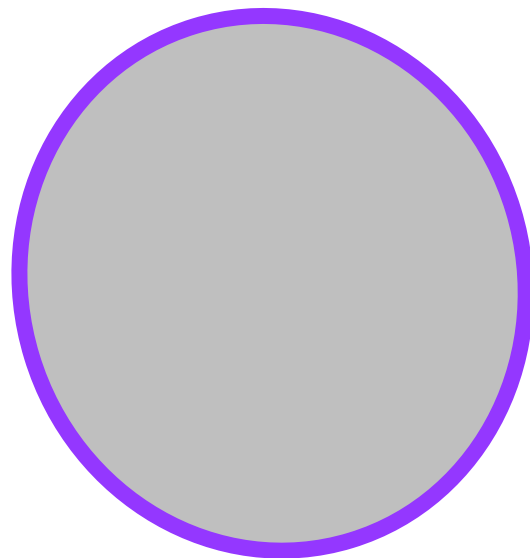
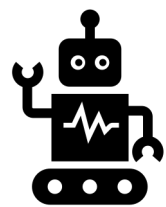


Collision avoidance



A constraint over

- Robot **pos**
- Human **pos** ellipsoid

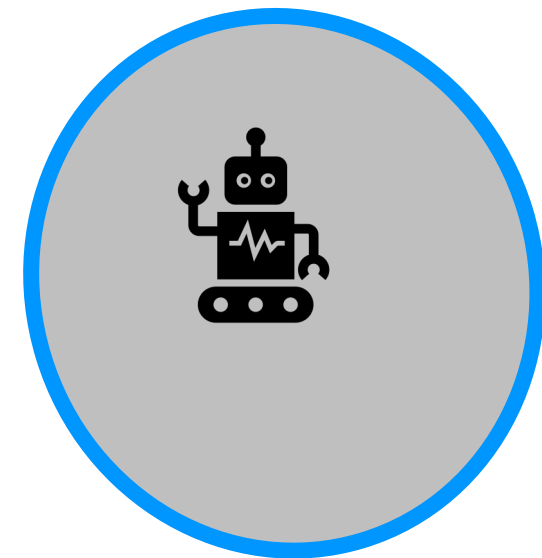
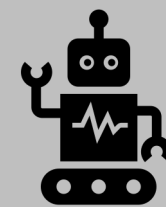


Safe impact

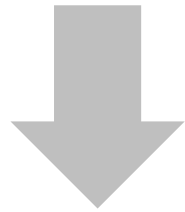


Constraints over

- Robot **vel**
- Human **vel** ellipsoid



Collision avoidance



A constraint over

- Robot **pos**
- Human **pos** ellipsoid

OR

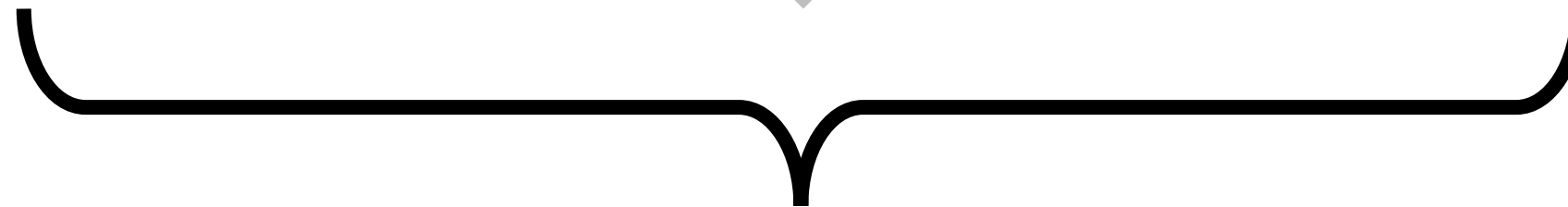


Safe impact



Constraints over

- Robot **vel**
- Human **vel** ellipsoid



Surrogate constraints

Human model



Gaussian Process



Ellipsoidal prediction

Collision avoidance

OR safe impact



Surrogate constraint



MPC

High probability safety guarantee

$$\Pr[\forall t \in \mathbb{N}, \text{safe}] > 1 - \delta$$

MPC + high probability
safety guarantee

Ensure human **safety**
&& Improve task **efficiency**

Collision avoidance
OR safe impact

$$d_{HR}^{max} = 0.085m$$



Safety = collision avoidance
OR safe impact

Safety = collision avoidance

MPC + high probability
safety guarantee

Ensure human **safety**

&& Improve task **efficiency**

Collision avoidance
OR safe impact